## Mathematical Discourse

## Help students work together to make sense of mathematics.

(1) What strategy did you use?
(2) Do you agree?
(3) Do you disagree?
(4) Would you ask the rest of the class that question?
${ }^{5}$ Could you share your method with the class?
(6) What part of what [student] said do you understand?
(7) Would someone like to share $\qquad$ ?
(8) Can you convince the rest of us that your answer makes sense?
© What do others think about what [student] said?
(10) Can someone retell or restate [student]'s explanation?
(11) Did you work together? In what way?
(12) Would anyone like to add to what was said?
(13) Have you discussed this with your group? With others?
(14) Did anyone get a different answer?
(15) Where would you go for help?
(16) Did everybody get a fair chance to talk, use the manipulatives, or be the recorder?
(17) How could you help another student without telling them the answer?
(18) How would you explain $\qquad$ to someone who missed class today?

## Help students rely more on themselves to determine whether something is mathematically correct.

(18) Is this a reasonable answer?
(20) Does that make sense?
(21) Why do you think that? Why is that true?
(27) Can you draw a picture or make a model to show that?How did you reach that conclusion?
(26) Does anyone want to revise their answer?
(26) How were you sure your answer was right?

## Help students learn to reason mathematically.

(26) How did you begin to think about this problem?
(23) What is another way you could solve this problem?
(23 How could you prove $\qquad$ ?
(20) Can you explain how your answer is different from or the same as [student]'s answer?Let's break the problem into parts. What would the parts be?Can you explain this part more specifically?Does that always work?Can you think of a case where that wouldn't work?How did you organize your information? Your thinking?

## Help students evaluate their own processes and engage in productive peer interaction.

(35 What do you need to do next?
(36) What have you accomplished?
(3)

What are your strengths and weaknesses?
(33) Was your group participation appropriate and helpful?

## Help students with problem comprehension.

(39) What is this problem about? What can you tell me about it?
(40) Do you need to define or set limits for the problem?
(4) How would you interpret that?
Could you reword that in simpler terms?Is there something that can be eliminated or that is missing?Could you explain what the problem is asking?What assumptions do you have to make?What do you know about this part?Which words were most important? Why?

## Mathematical Discourse

## Help students learn to conjecture, invent, and solve problems.

(38 What would happen if ?
(70) Do you see a pattern?
(50) What are some possibilities here?
(2) Where could you find the information you need?
(3)

How would you check your steps or your answer?
(3) What did not work?How is your solution method the same as or different from [student]'s method?
Other than retracing your steps, how can you determine if your answers are appropriate?
How did you organize the information?
Do you have a record?
(3)

How could you solve this using tables, lists, pictures, diagrams, etc.?
What have you tried? What steps did you take?
How would it look if you used this model or these materials?
How would you draw a diagram or make a sketch to solve the problem?Is there another possible answer? If so, explain.
2 Is there another way to solve the problem?Is there another model you could use to solve the problem?Is there anything you've overlooked?
How did you think about the problem?What was your estimate or prediction?
How confident are you in your answer?
What else would you like to know?What do you think comes next?
Is the solution reasonable, considering the context?Did you have a system? Explain it.
Did you have a strategy? Explain it.
3 Did you have a design? Explain it.

## Help students learn to connect mathematics, its ideas, and its application.

(44) What is the relationship between $\qquad$ and $\qquad$ ?
(36) Have we ever solved a problem like this before?
(c) What uses of mathematics did you find in the newspaper last night?
(21) What is the same?
(38) What is different?
(20) Did you use skills or build on concepts that were not necessarily mathematical?Which skills or concepts did you use?What ideas have we explored before that were useful in solving this problem?
(32) Is there a pattern?Where else would this strategy be useful?
(84) How does this relate to $\qquad$ ?
(35) Is there a general rule?
(88) Is there a real-life situation in which this could be used?How would your method work with other problems?
(38) What other problem does this seem to lead to?

## Help students persevere.

Have you tried making a guess?What else have you tried?Would another method work as well or better?Is there another way to draw, explain, or say that?Give me another related problem. Is there an easier problem?How would you explain what you know right now?
## Help students focus on the mathematics from activities.

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[^0]:    (55)

    What was one thing you learned (or two, or more)?
    

    Did you notice any patterns? If so, describe them.
    (37) What mathematics topics were used in this investigation?What were the mathematical ideas in this problem?
    ©9 What is mathematically different about these two situations?
    $(100$ What are the variables in this problem? What stays constant?

